Interaction Dynamics of High Reynolds Number Magnetized Plasma Flow on the CTIX Plasma Accelerator

by

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Abstract

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Doctor of Philosophy in Plasma Physics

University of California, Davis

Professor David Hwang, Chair

Compact Toroid Injection eXperiment defined

broad, simple description of project

Professor David Hwang
Dissertation Committee Chair

Dedication

Acknowledgments

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